

Thursday, February 14

• quiz #1 due

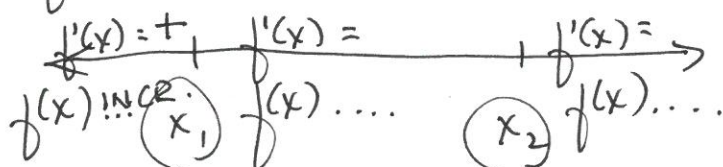
• 2.1: FIRST DERIV

① find y'

② $y' = 0$; y' UNDEF

(critical values ... critical points) $\rightarrow (x_1, f(x_1)) (x_2, f(x_2))$

③ $f'(x)$: (SIGN CHART)



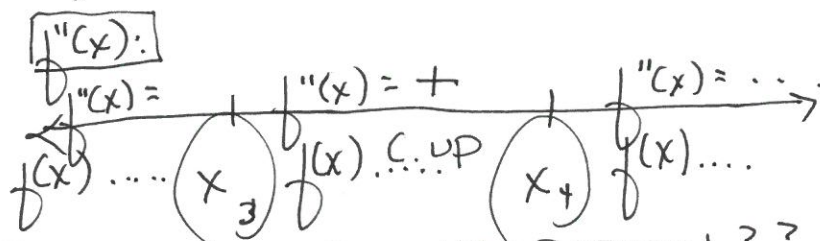
④ REL MAX/MIN; ABSOLUTE MAX/MIN

• 2.2: SECOND DERIV

① find y''

② $y'' = 0$; y'' UNDEF

③ $f''(x)$: (SIGN CHART)

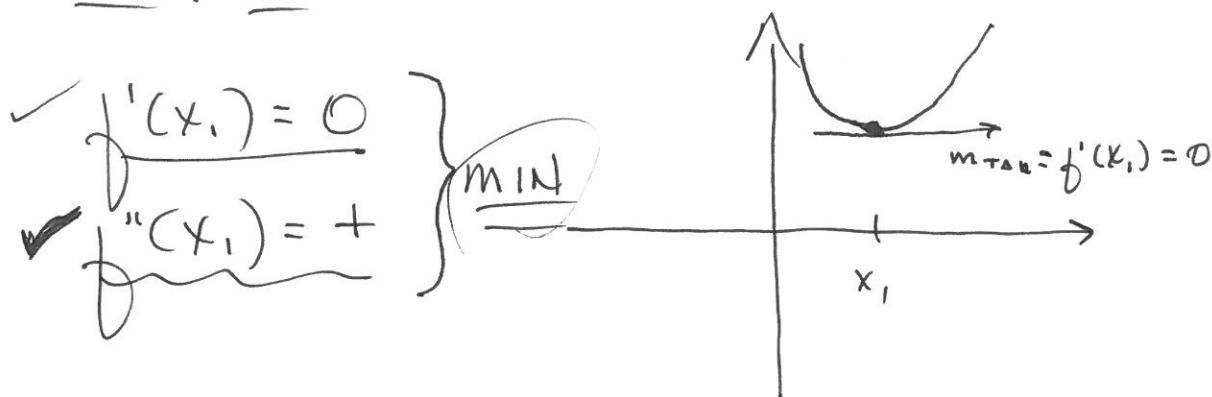


④ POINTS OF INFLECTION ??

changes concavity there

• today (2.3; 2.4)

2.1 & 2.2:



2.3: Comprehensive Graphing $y = \frac{f(x)}{g(x)}$

1.) vertical asymptotes

$g(x) = 0$

$x = k$

2.) horizontal asymptotes

$y = k$

$\lim_{x \rightarrow \infty} \frac{f(x)}{g(x)} = \text{---}$

3.) "hole" in the graph:

$y = \frac{(x-4)(x+1)}{(x-4)(x-5)}$ $x \neq 4$



$y = \frac{x+1}{x-5}$

VA: $x = 5$

HA: $y = 1$

hole: $(4, \frac{5}{-1}) = (4, -5)$

4.) slant or oblique
asymptote

oblique asymptote:

$$y = \frac{x^2 + 4x - 3}{x + 5}$$

H.A.: $\lim_{x \rightarrow \infty} \frac{x^2 + 4x - 3}{x + 5} = \lim_{x \rightarrow \infty} \frac{x^2}{x} = \lim_{x \rightarrow \infty} x = \infty$
(no H.A.)

$$\begin{array}{r} x - 1 + \frac{2}{x+5} \\ \underline{x+5 \overline{) x^2 + 4x - 3}} \\ -(x^2 + 5x) \\ \hline -1x - 3 \\ \underline{-(-1x - 5)} \\ +2 \end{array}$$

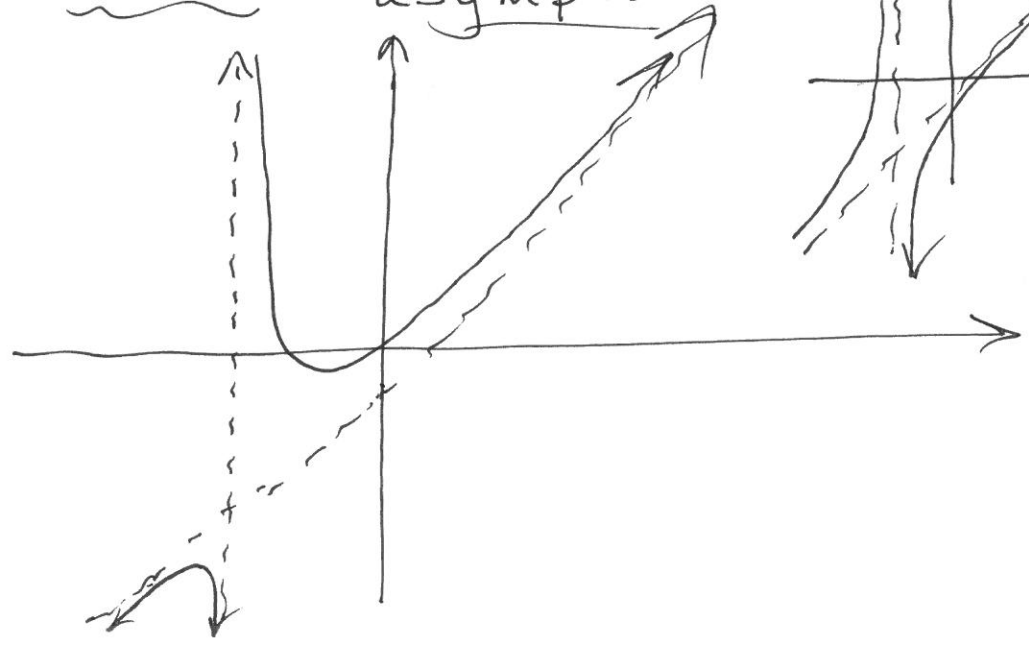
$$y = \frac{x^2 + 4x - 3}{x + 5} = x - 1 + \frac{2}{x + 5}$$

V.A.: $x = -5$

H.A.: none

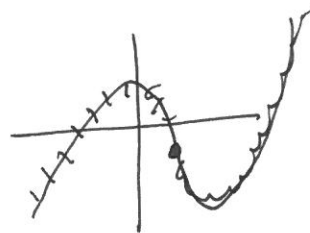
$$y = x - 1 + \frac{2}{x + 5} \quad x \rightarrow \infty$$

$y = x - 1$ oblique asymptote



(4)

intercepts

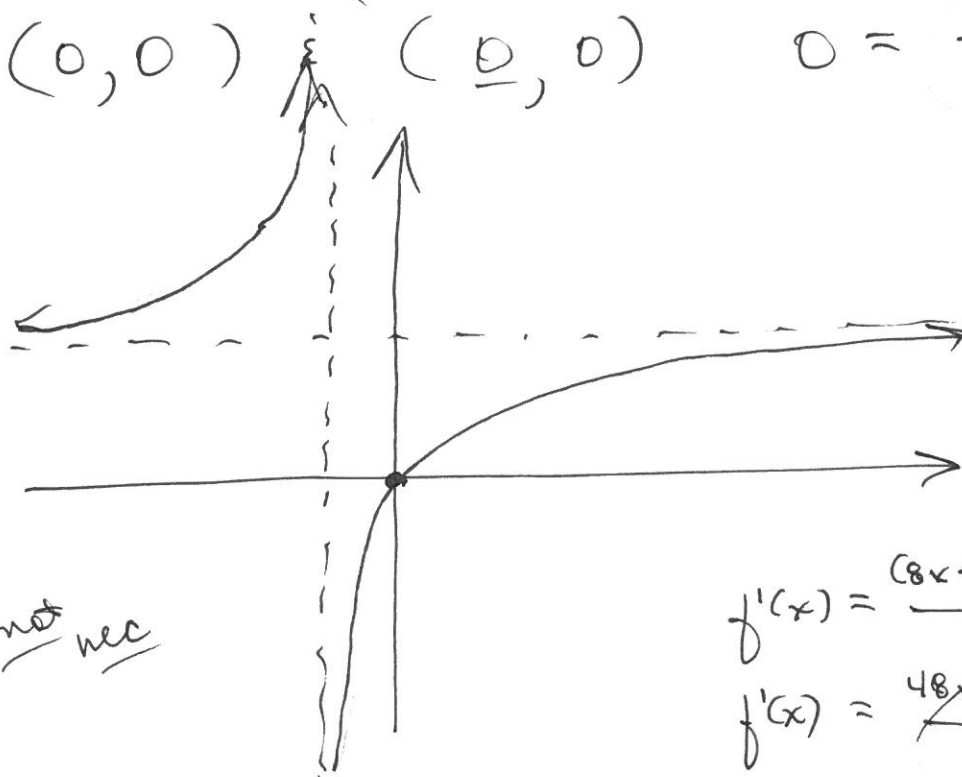
① x-int: (set $y=0$)② y-int: (set $x=0$) y' & y'' information

ex: $f(x) = \frac{6x}{8x+3}$

V.A.: $x = -\frac{3}{8}$
H.A.: $y = \frac{3}{4}$

int: $(0,0)$ $(\underline{0}, 0)$

$0 = \frac{6x}{8x+3}$ $6x=0$
 $x=0$



$f''(x) = \text{not nec}$

$$f'(x) = \frac{(8x+3)(6) - (6x)(8)}{(8x+3)^2}$$

$$f'(x) = \frac{48x+18 - 48x}{(8x+3)^2}$$

$$f'(x) = \frac{18}{(8x+3)^2} = \frac{+}{+} = +$$

(w/entire graph)

ex:

$$f(x) = \frac{x^2 + x - 2}{2x^2 - 2} = \frac{(x+2)(x-1)}{2(x^2-1)}$$

$$f(x) = \frac{(x+2)(x-1)}{2(x+1)(x-1)}$$

$x=1$ "hole"

$$f(x) = \frac{(x+2)}{2(x+1)}$$

V.A.: $x = -1$

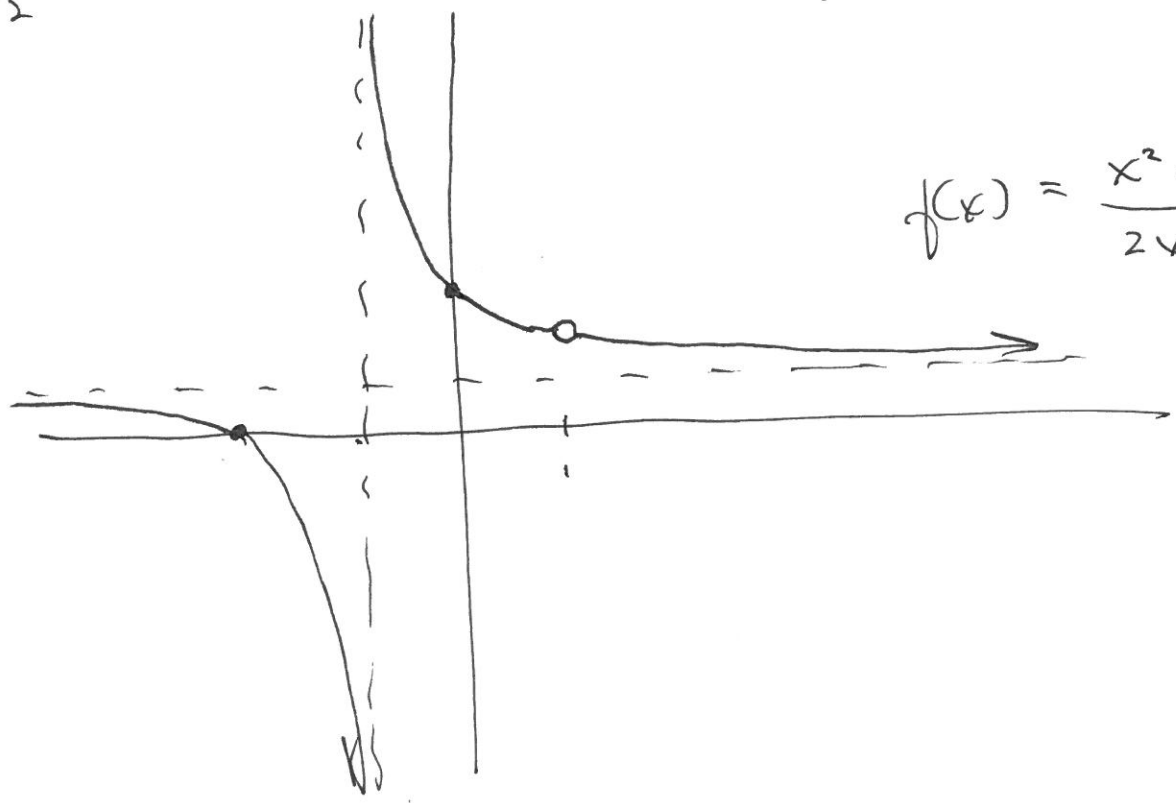
H.A.: $y = \frac{1}{2}$

int: $(0, 2)$
 $(-2, 0)$

$$\frac{0}{4} \quad \frac{0}{11}$$

$$\frac{0}{52}$$

$$0 = \frac{(x+2)}{2(x+1)} \quad x+2=0 \quad x=-2$$

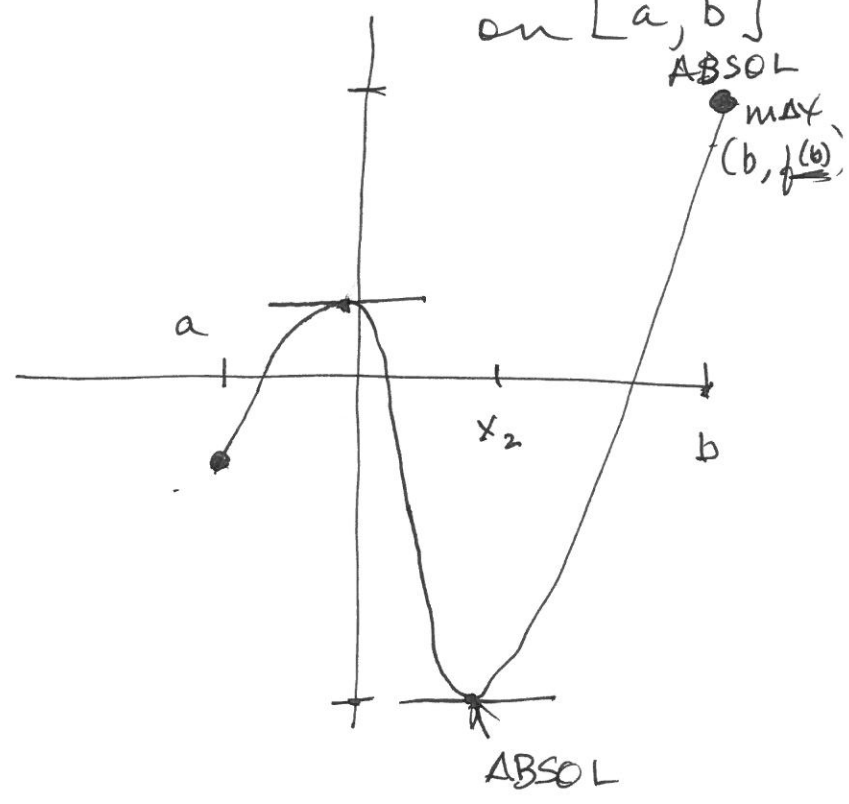
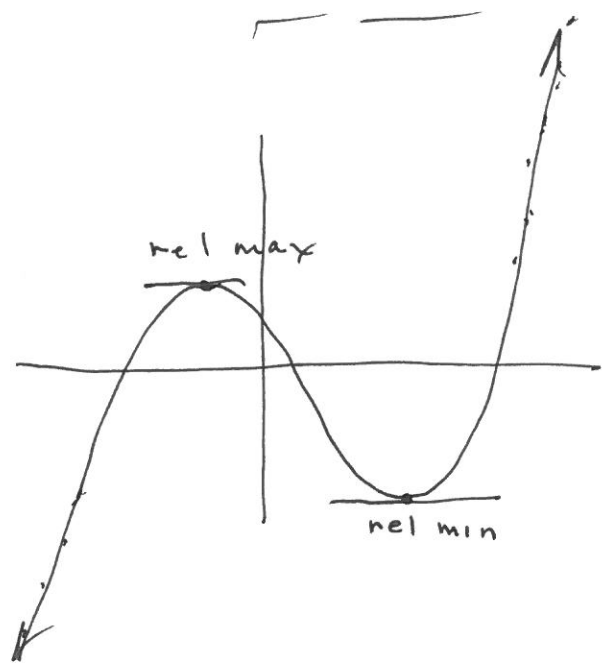


$$f(x) = \frac{x^2 + x - 2}{2x^2 - 2}$$

2.4: ABSOLUTE MAX/MINS ON

A CLOSED INTERVAL (ENDPTS)

on $[a, b]$



ABSOL MIN
(lowest y-value)

find the absolute max/min

value of the function

(highest y-value)
(lowest y-value)

ex: $f(x) = x^3 - 3x$ ✓ on $[-5, 2]$ ✓ ⑦

$$f'(x) = 3x^2 - 3$$

$$f'(x) = 3(x^2 - 1)$$

$$f'(x) = 3(x-1)(x+1)$$

① endpoints ✓

② critical pts

① $f'(x) = 0$

$$0 = 3(x-1)(x+1)$$

$$x = 1 ; x = -1$$

$$(1, -2) \quad \frac{1}{2} \quad (-1, +2)$$

$$1^3 - 3(1)$$

$$(-1)^3 - 3(-1)$$

$$-1 + 3$$

② ~~$f'(x)$ undefined.~~

endpts

$$(-5, -110)$$

$$(-5)^3 - 3(-5)$$

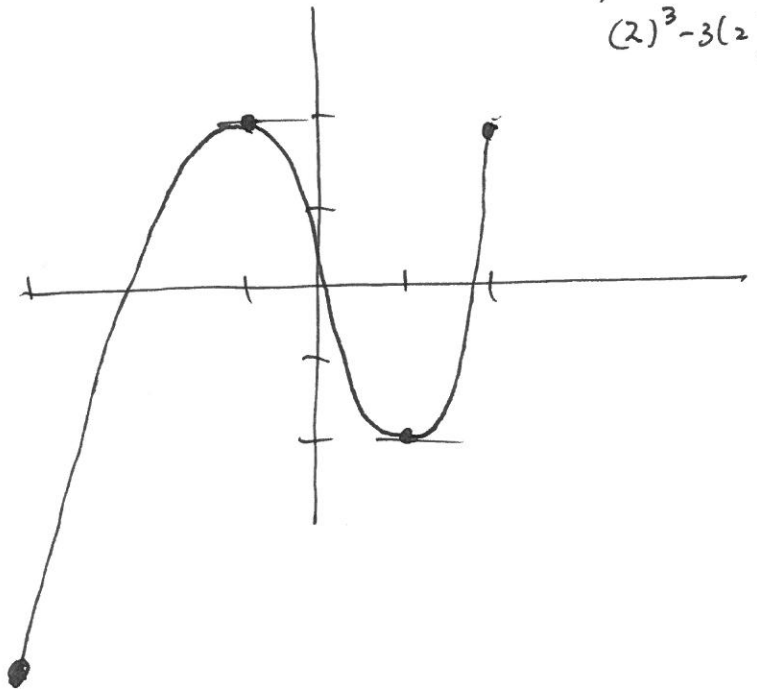
$$-125 + 15$$

$$(2, 2)$$

$$(2)^3 - 3(2)$$

max. value
of the function
2

min value
of the function
-110



$$f(x) = \underline{2x} + \left(\frac{72}{x} \right) \quad (0, +\infty)$$

$$f'(x) = 2 + 72(-1 \cdot x^{-2})$$

$$f'(x) = \boxed{2 - \frac{72}{x^2} = 0}$$

ABS MIN
24

$$(6, 24)$$

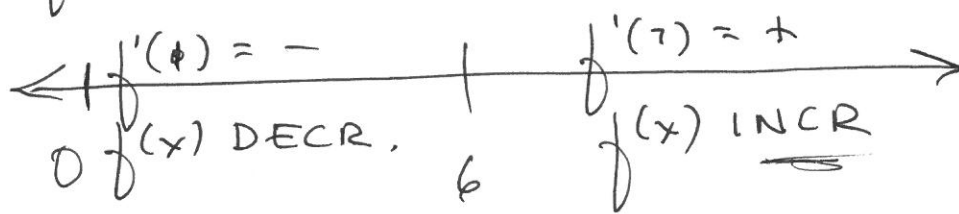
$$2(6) + \frac{72}{6}$$

$$\frac{2}{1} = \frac{72}{x^2}$$

$$\frac{2x^2}{2} = \frac{72}{2}$$

$$x^2 = 36 \quad x = \pm 6 \rightarrow \underline{\underline{+6}}$$

$f'(x):$



In each problem, find $f'(x)$ using the recommended technique; simplify completely. Due at the beginning of class on Thursday, February 14. You can use the book, your notes. You are to work **individually** on this quiz. Turn in this sheet with work and answers:

1.) $f(x) = 8x^3 + 4\sqrt[3]{x} - \frac{5}{x^2} + 17$ (power rule) $f(x) = 8x^3 + 4x^{1/3} - 5x^{-2} + 17$

$$f'(x) = 8(3x^2) + 4\left(\frac{1}{3} \cdot x^{-2/3}\right) - 5(-2 \cdot x^{-3}) + 0$$

$$f'(x) = 24x^2 + \frac{4}{3}x^{-2/3} + 10x^{-3}$$

2.) $f(x) = \frac{5x-3}{2x+1}$ (quotient rule)

$$f'(x) = \frac{(2x+1) \cdot (5) - (5x-3) \cdot (2)}{(2x+1)^2} = \frac{10x+5-10x+6}{(2x+1)^2}$$

$$f'(x) = \frac{11}{(2x+1)^2}$$

3.) $f(x) = (2x+5)(3x^2-4x+1)$ (product rule)

$$f'(x) = (2x+5)(6x-4) + (3x^2-4x+1)(2)$$

$$f'(x) = 12x^2 + 30x - 8x - 20 + 6x^2 - 8x + 2$$

$$f'(x) = 18x^2 + 14x - 18$$

4.) $f(x) = \sqrt{3x^2+4x}$ (chain rule or extended power rule) $f(x) = (3x^2+4x)^{1/2}$

$$f'(x) = \frac{1}{2}(3x^2+4x)^{-1/2} \cdot (6x+4)$$

$$f'(x) = (3x+2)(3x^2+4x)^{-1/2}$$